



Review

The role of lanthanides in TiO₂-based photocatalysis: A review

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ABSTRACT

This review provides an in-depth analysis of lanthanide-titania-modified semiconductor photocatalysts (Er-, Ho-, Nd- and Tm-TiO₂) for the photocatalytic degradation of organic pollutants under UV and visible light irradiation. In the first section, the unique properties of the lanthanides are summarized. In the second section, the influence of the preparation methods and surface properties of the selected rare earth metals (RE) on the photocatalytic activity of TiO₂ was surveyed. In the third section, the mechanism of the RE-TiO₂ visible light photoactivity was described. Finally, first-principles computer simulations of the RE-TiO₂ structure and energy along with the influence of the anti-Stokes up-conversion process on the photocatalytic activity of the RE-TiO₂ were discussed in detail.

1. Introduction

In recent years, environmental contamination has become a fundamental problem worldwide. In this regard, photocatalysis has been proposed as an environmentally friendly approach and a promising method to remove pollutants from water and air due to the possible oxidation of organic pollutants to CO₂ and H₂O. Titanium dioxide is the earliest discovered and most widely investigated photocatalyst as a result of its high photoactivity, relatively low cost, low toxicity and good chemical and thermal stability [1,2]. Unfortunately, TiO₂ is sensitive only to UV light by cause of its large band gap, and it has low quantum efficiency, resulting from the fast recombination rate of photogenerated electron-hole pairs. Various strategies of modifying TiO₂ have been applied to overcome the abovementioned drawbacks, such as metal and non-metal doping, surface modification by dyes, noble metal nanoparticles or narrow band gap semiconductor particles [1–14]. Among these strategies, the preparation of TiO₂ modified with rare earth (RE) metals appears to be a highly efficient method to tune the response of the semiconductor to the visible light region and to enhance its photocatalytic properties [15–18]. The current reviews on rare earth metal-modified TiO₂ (RE-TiO₂) focus on the preparation methods and characterization of the photocatalysts [19], the photocatalytic degradation of organic molecules and the photosplitting of water in the presence of RE-TiO₂ [17], La, Ce, Eu, and Gd-TiO₂ [15], the use of Gd-TiO₂ for photoenergy applications [16], the use of RE-TiO₂ for the photocatalytic remediation of wastewater [18], visible-to-ultraviolet

up-conversion processes [20] and thin lanthanides-TiO₂ films produced by spray-deposition [21]. However, it is still not clear how lanthanides affect visible light response of TiO₂-based photocatalysts. In view of this, this review covers important aspects related to the photocatalytic activity mechanism over selected (Er³⁺, Ho³⁺, Nd³⁺ and Tm³⁺) RE-TiO₂ photocatalysts and the relationship between the mechanism and the anti-Stokes up-conversion process. Moreover, a computational description of the electronic structure and optical properties is provided to offer possible suggestions to researchers in this field for the design of new materials supported by computational methods. The preparation methods and surface properties of RE-TiO₂ are also discussed in detail.

2. Unique properties of lanthanides

Rare earth metals have shown great potential as TiO₂ dopants not only in the red shift of absorption but also in increasing the temperature of the anatase to rutile transformation and in the ability to form complexes with various Lewis bases, e.g., alcohols, aldehydes, acids, amines, and thiols [9,22,23]. Additionally, materials (such as TiO₂) modified by RE³⁺ ions usually present luminescent properties. Trivalent lanthanide ions with ladder-like energy levels embedded in an appropriate inorganic host lattice can emit UV or visible light through the sequential absorption of multiple near-infrared photons [20,24]. This process, which can result in the transformation of light from the near-infrared and visible spectral range to the ultraviolet wavelengths, could be used to excite wide band semiconductor, such as TiO₂ [25].

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The lanthanides collectively consist of 15 elements starting with atomic number 57 (lanthanum) to 71 (lutetium). Scandium and yttrium are chemically similar; thus, finally 17 elements constitute the rare earth series. The luminescence of rare earth ions arises from the *f-f* electronic transitions within their partially filled *4f* orbitals. These orbitals are sterically shielded from the surrounding microenvironment by the filled *5s* and *5p* orbitals, meaning that there are almost no perturbations of these transitions. Thus, these transitions appear as several narrow emission bands specific for the emitting lanthanide ion. This phenomenon gives the lanthanides unique chemical properties in photocatalytic applications [26,27]. Only four main lanthanide ions can theoretically activate the TiO_2 photocatalyst through the Vis-to-UV or NIR-to-UV up-conversion process, namely, Er^{3+} , Ho^{3+} , Nd^{3+} and Tm^{3+} . Simplified energy level diagrams of these RE ions and the excitation path for the up-conversion emission in the UV range are presented in Fig. 1. The up-conversion process can be achieved through the chains of the ground state absorption (GSA) and excited state absorption (ESA) [11]. During the anti-Stokes process, two or more photons are absorbed sequentially by a material to reach an excited state, and one higher-energy photon can be released [20]. For this reason, only the TiO_2 doped by Er, Ho, Nd and Tm was described in the review and an attempt was made to correlate activity of these photocatalysts with their up-conversion properties.

3. Preparation methods and surface properties of RE- TiO_2

3.1. Erbium- TiO_2

3.1.1. Synthesis and morphology of Er- TiO_2

Generally, Er- TiO_2 can be obtained by hydro/solvothermal treatment, sol-gel methods and electrospinning, as shown in Table 1. Recent literature has revealed that the hydro/solvothermal and sol-gel methods are still some of the most commonly used synthesis methods for the preparation of Er- TiO_2 (see Table 1); these types of methods have become increasingly popular as straightforward, cost-effective preparation processes to produce Er- TiO_2 with high purity at a relatively low temperature.

In all applications, Er- TiO_2 photocatalysts have been employed in the form of various morphologies including zero-dimensional (nanoparticles), one-dimensional (nanotubes) or two-dimensional (nanobelts) structures, as shown in Figs. 2 and 3 and Table 1. These morphologies determine the physical and structural properties of RE- TiO_2 as well as its luminescence and photocatalytic properties. To prepare Er- TiO_2 , titanium(IV) isopropoxide, titanium(IV) butoxide, TiO_2 colloidal solution can be used as TiO_2 precursors, while $\text{Er}(\text{NO}_3)_3 \cdot x\text{H}_2\text{O}$, ErCl_3 and Er_2O_3 could serve as erbium precursors [28–35].

Among all the synthesis methods, magnetron sputtering [36], spin coating [37], implantation [38], and anodic [10,39] and thermal plasma oxidation [40] are infrequently used. Most of these methods (such as spin coating and magnetron sputtering) produce Er- TiO_2 photocatalysts as a thin layer. Moreover, the electrochemical oxidation of Ti foil in the presence of $\text{Er}(\text{NO}_3)_3$ in the ammonium fluoride/ethylene glycol organic electrolyte, allows formation of oriented nanotube arrays modified with erbium ions (one dimensional) [39].

In addition, most of the doping strategies have no influence on the morphology of the obtained Er- TiO_2 ; thus, a direct comparison of the photoactivity between the pristine and modified samples is reliable. However, in some cases, the morphology of the TiO_2 photocatalyst appears to be slightly influenced by the presence of Er ions. Obregón and Colón [41] found that the synthesis route they applied for the preparation of Er- TiO_2 photocatalysts produces a homogeneous distribution of round particles with sizes below 15 nm, but as the Er^{3+} content increases, the average size progressively decreases, reaching a value of 10 nm for 4 at.% Er^{3+} .

3.1.2. Crystal structure of Er- TiO_2

It is well known that one of the major factors that greatly influences the properties of the modified photocatalysts is the crystal structure, namely, the crystallite size and unit cell parameters. Yang et al. [42] prepared Er-doped TiO_2 nanofibrous films via an electrospinning method and observed that the crystallite size decreased from 17.9 to 8.1 nm as the erbium content introduced into TiO_2 increased from 0 (pristine) to 1.5 mol% (doped). They also found that the cell parameters of Er- TiO_2 were similar to pristine TiO_2 . These results demonstrated that Er^{3+} species exist at the crystal boundary rather than in the inner crystalline structure of TiO_2 due to the substitution of a small Ti ion (68 pm) by a large Er ion (100 pm) causes an increase in the lattice parameters and a shift in the diffraction patterns [42]. A similar effect was found by Falcomer et al. [44] in which the crystallite size decreased from 30 to 16 nm after erbium doping, while the unit cell volume for the Er- TiO_2 sample was close to that of the pristine anatase TiO_2 . The observed changes were attributed to the presence of lanthanide ions in the TiO_2 host, which led to strain and stress in the lattice [44]. Note that Li et al. [39] prepared Er-doped TiO_2 nanotubes and observed that the diffraction peaks of the doped photocatalyst moved to the left. Based on Bragg's law, they concluded that the left translation of the diffraction peaks indicated that the Er^{3+} was successfully introduced into the lattice of the TiO_2 nanotubes [39].

Another crucial point that should be mentioned, it is the effect of erbium doping on the hindrance of the phase transition of anatase to rutile. Several reports have demonstrated this phenomenon, when erbium ions were incorporated into TiO_2 lattice [41,42]. Yang et al. [42] observed that doping by erbium ions inhibited the appearance of the rutile phase when calcined at the same temperature 500 °C. It was proposed that this inhibition may occur due to the stabilization of the anatase phase by the surrounding rare earth elements through the formation of Ti-O-rare earth element bonds. The interaction between the different tetrahedral Ti atoms or between the tetrahedral Ti and the octahedral Ti prevents the phase transformation into rutile [42].

3.1.3. BET surface area and optical properties of Er- TiO_2

In reference to the BET surface area, Er- TiO_2 photocatalysts exhibit relatively high values; in all cases, the surface area was slightly higher than that of pristine TiO_2 (see Table 1). It was observed that the BET surface area progressively increased as the erbium content increased from 102 (for pristine TiO_2) to 116 m²/g (for TiO_2 containing 4 at.% of Er) [41]. At the same time, it was observed that the pore size presents a narrow distribution, with an average pore size of 9–12 nm with increasing average values as the erbium content increased [34]. In contrast to the BET surface area, the literature data did not provide clear information about the band structure of erbium-modified TiO_2 photocatalysts. Some authors have observed a decrease in the band gap of Er- TiO_2 , while other authors have found that the calculated band gap of Er- TiO_2 appeared to be similar to that of pristine TiO_2 (see Table 1). Therefore, the presence of erbium may or may not affect the band structure of the anatase structure. For example, Obregón et al. [34] and Mazierski et al. [10] found that erbium doping did not notably affect the absorption edge of TiO_2 . Furthermore, they observed a small and progressive blue shift (after doping). A similar effect was also observed by Yang et al. [42] in which Er- TiO_2 photocatalysts were prepared using an electrospinning technique. These results are opposite to those found by Castaneda-Contreras et al. [31] for Er- TiO_2 systems prepared by the sol-gel method. They suggested that the incorporation of erbium into the structure induced a marked redshift and the subsequent narrowing of the band gap values. The improvement in the photoactivity was mainly attributed to the lower band gap values and, to a lesser extent, to energy transfer from Er^{3+} to TiO_2 . Comparable results to that of Castaneda-Contreras et al. [31] were observed by Lee et al. [37]; namely, the energy gap values were 3.25, 2.85, 2.85, 2.85, 2.81, and 2.89 eV for 0, 0.1, 0.3, 0.5, 0.7 and 1.0 mol% of Er, respectively. In conclusion, the literature data are not consistent, and this aspect should

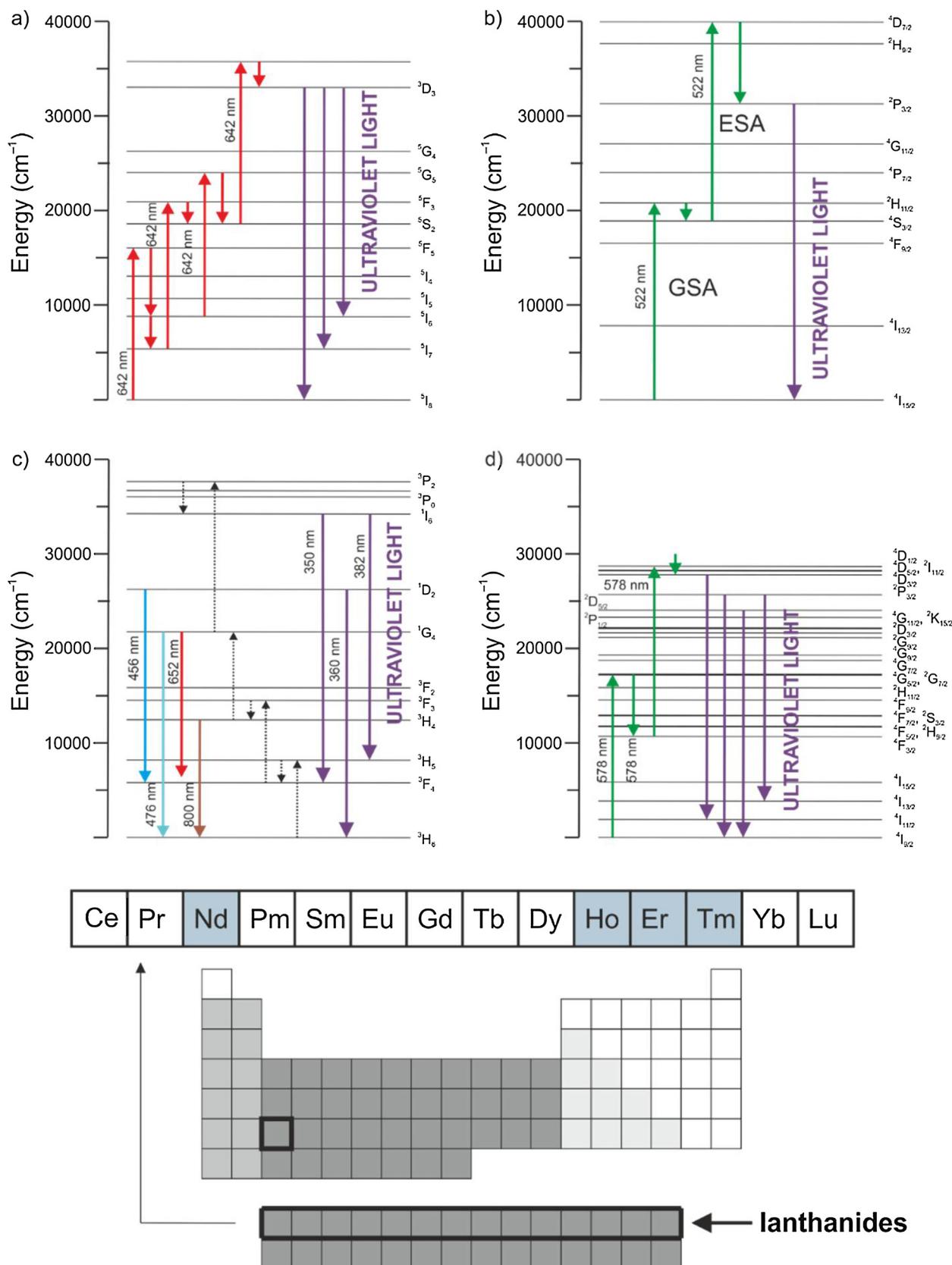


Fig. 1. Simplified energy level diagrams of an excitation path for the up-conversion emission of ultraviolet light: a) Ho³⁺ under 642 nm excitation, b) Er³⁺ under 522 nm excitation, c) Tm³⁺ under 980 nm excitation, and d) Nd³⁺ under 578 nm excitation; GSA - ground state absorption, ESA - excited state absorption.

Table 1
The structural and physical properties of Er-TiO₂ photocatalysts and description of photocatalytic system used to estimate photocatalytic activity.

No.	Preparation method/obtained structure	Localization of RE species	Chemical characteristics of RE species	Unit cell parameters	BET Surface area (m ² /g)	Band-gap (eV)	Photocatalytic activity set -up	Up-conversion measurements	Ref.
1.	Sol-gel Thin film	Doping	Ion	No data	No data	No data	Not tested	$\lambda_{\text{ex}} = 800 \text{ nm}$ $\lambda_{\text{em}} = 410, 525, 548 \text{ and } 660 \text{ nm}$	[45]
2.	Magnetron sputtering Thin film	Doping	Ion	No data	No data	No data	Not tested	$\lambda_{\text{ex}} = 980 \text{ nm}$ $\lambda_{\text{em}} = 490 \text{ and } 670 \text{ nm}$	[36]
3.	Electrospinning	Doping	Ion	136.28 - pristine TiO ₂	No data	Blue shift	Model contaminant: methylene blue	Not tested	[42]
4.	Hydrothermal Nanofibrous film	Doping (interstitial)	Oxidation state	136.69 - Er-TiO ₂ 136.30 - pristine TiO ₂	102 - pristine TiO ₂ 110 - Er-TiO ₂	3.16 - pristine TiO ₂ 3.18 - Er-TiO ₂	Irradiation source: 500 W Xe lamp Model contaminant: Phenol, toluene and methylene blue	$\lambda_{\text{ex}} = 980 \text{ nm}$ $\lambda_{\text{em}} = 390 \text{ and } 415 \text{ nm}$	[34]
5.	Hydrothermal assisted sol-gel Nanopowder	Doping	Ion	No data	No data	No data	Not tested	$\lambda_{\text{ex}} = 980 \text{ nm}$ Up-conversion was not detected	[35]
6.	Sol-gel Thin film Solothermal	Doping	Ion	No data	No data	No data	Not tested	$\lambda_{\text{ex}} = 330 \text{ nm}$ $\lambda_{\text{em}} = 614 \text{ nm}$	[29]
7.	Nanoparticles Hydrothermal Nanobelts	Doping (substitutional)	Ion	136.20 - pristine TiO ₂	No data	No data	Not tested	$\lambda_{\text{ex}} = 488 \text{ nm}$	[44]
8.	Nanoparticles Hydrothermal Nanobelts	Doping	Ion	136.74 - Er-TiO ₂ No data	No data	No data	Not tested	$\lambda_{\text{em}} = 550, 660 \text{ and } 860 \text{ nm}$ $\lambda_{\text{ex}} = 980 \text{ nm}$ $\lambda_{\text{em}} = 520-570 \text{ and } 630-680 \text{ nm}$	[43]
9.	Sol-gel Nanoparticles	Doping (substitutional)	Ion	No data	No data	No data	Not tested	$\lambda_{\text{ex}} = 980 \text{ nm}$ $\lambda_{\text{em}} = 439, 488, 536, 565 \text{ and } 664 \text{ nm}$	[30]
10.	Electrospinning	Doping	Ion	No data	No data	No data	Model contaminant: Phenol, methyl orange and rhodamine B	Not tested	[46]
304							Irradiation source: 500 W Xe lamp and LEDs (517-522 nm)	$\lambda_{\text{ex}} = 350 \text{ nm}$ $\lambda_{\text{em}} = 650 \text{ and } 720 \text{ nm}$	[47]
11.	Electrospinning Nanofibers	Doping (substitutional)	Ion	No data	No data	Blue shift	Not tested	$\lambda_{\text{ex}} = 488 \text{ nm}$ $\lambda_{\text{em}} = 1534 \text{ and } 613 \text{ nm}$	[32]
12.	Sol-gel	Doping	Ion	No data	No data	3.2 - pristine TiO ₂ 3.0 - Er-TiO ₂	Model contaminant: Methylene blue	Not tested	[31]
13.	Nanoparticles Thermal plasma oxidation	Doping	New phase Er ₂ Ti ₂ O ₇	No data	No data	No data	Irradiation source: Deuterium-tungsten (Vis)	Not tested	[40]
14.	Sol-gel Thin film	Doping (interstitial)	Ion	No data	No data	No data	Model contaminant: Methylene blue	$\lambda_{\text{ex}} = 350 \text{ nm}$ $\lambda_{\text{em}} = 650 \text{ and } 720 \text{ nm}$	[32]
15.	Anodization Nanotubes	Doping (substitutional)	Ion	Increased	No data	No data	Irradiation source: 160 W Hg lamp	Not tested	[39]
16.	Sol-gel Nanoparticles	Doping	Ion	No data	No data	Red shift	Model contaminant: Orange I	Not tested	[33]
17.	Spin coating	Doping	Ion	No data	No data	3.25 - pristine TiO ₂	Irradiation source: 8 W Hg lamp (UV) and 70 W sodium lamp (Vis)	Not tested	[37]
Thin film Hydrothermal	Doping (substitutional)	Ion	No data	102 - pristine TiO ₂ 110 - Er-TiO ₂	2.81 - Er-TiO ₂ 3.16 - pristine TiO ₂ 3.18 - Er-TiO ₂	Model contaminant: Phenol and methylene blue	Not tested	$\lambda_{\text{ex}} = 488 \text{ nm}$ $\lambda_{\text{em}} = 1534 \text{ and } 613 \text{ nm}$	[48]
Nanoparticles							Irradiation source: 200 W Hg-Xe lamp (UV-Vis-IR, UV-Vis, Vis and Vis-IR)		

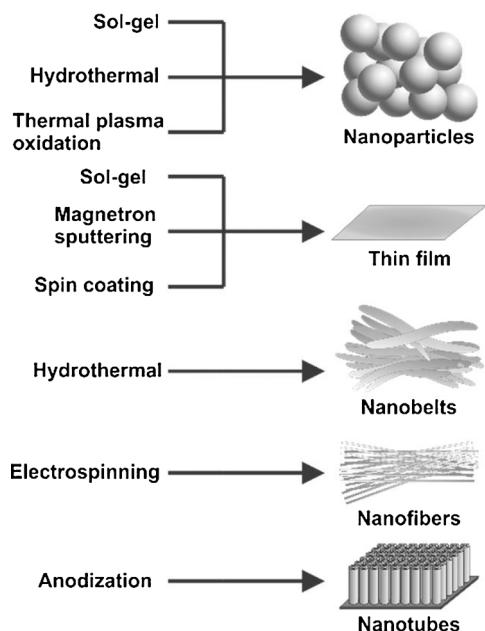


Fig. 2. Schematic illustration of the Er-TiO₂ morphologies obtained by sol-gel, hydrothermal, thermal plasma oxidation, spin coating electrospinning and anodization methods.

be clarified in the future. Additionally, for erbium-doped photocatalysts, different lines appear in the range of 400–700 nm compared to the TiO₂ absorption spectra, and those lines can be associated with the excitation of the erbium species. The absorption lines located at

approximately 489, 520, and 653 along with a small tail at 800 nm correspond to the transitions from the Er³⁺ ground state $^4I_{15/2}$ to the higher energy levels of $^4F_{7/2}$, $^4H_{11/2}$, $^4F_{9/2}$ and $^4G_{9/2}$, respectively [31,33,34].

3.1.4. Up-conversion properties of Er-TiO₂

The up-conversion properties of the Er-TiO₂ photocatalysts have often been studied. In the case of NIR irradiation, the presence of erbium appears to promote the up-conversion process, pumping photons into the UV range in the TiO₂ structure (as shown in Fig. 2). It was reported that Er-TiO₂ shows a weak UV photoluminescence (PL) emission at approximately 390–410 nm after excitation at 980 nm [34]. This up-conversion process involves a sequential three-photon absorption ($^4I_{15/2} \rightarrow ^4I_{11/2}$, $^4I_{11/2} \rightarrow ^4F_{7/2}$ and $^4S_{3/2} \rightarrow ^2G_{7/2}$). Then, by multiphoton relaxation, the $^2G_{7/2}$ excited state decays to the lower $^2G_{11/2}$ and $^2H_{9/2}$ states. The photoluminescence emission in the UV range is then produced by the $^2G_{11/2} \rightarrow ^4I_{11/2}$ transition, giving a feeble emission at approximately 390–400 nm [34]. Therefore, the improvement of the photocatalytic efficiency might be related to the increasing number of available photons with an appropriate energy. Obregón et al. [34] found that by exciting the Er-TiO₂ photocatalyst with 980 nm light, PL spectra in the UV region show two weak emission bands located at approximately 390/3.18 and 415/4.14 nm/eV. In contrast to these results, Mao et al. [36] observed only a 490 nm green emission and a 670 nm red emission after excitation of the Er-TiO₂ thin film by a laser of 980 nm. Bahtat et al. [28] studied the up-conversion properties of the Er-TiO₂ samples in the form of planar waveguides obtained by sol-gel method followed by dip-coating. In this case, four broad bands were observed at approximately 410, 525, 548, and 660 nm. However, Salhi and Deschanvres [35] obtained RE-TiO₂ nanopowders, which exhibited

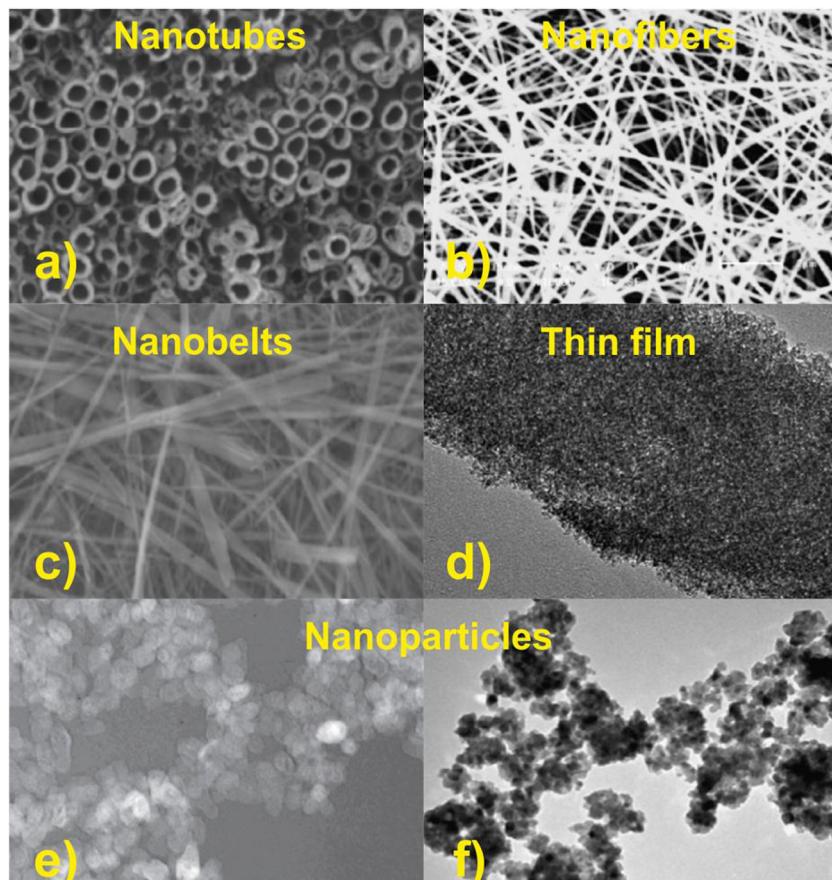


Fig. 3. (a–c) SEM and (d–f) TEM images of the Er-TiO₂ morphologies based on [30,32,34,39,42,43]. Reprinted with permission from ref [30,32,34,39,42,43]. Copyright 2009, 2010, 2012, 2014 Elsevier Inc.

strong, weak and very weak emission bands located at 550, 525 nm (green region) and 655 nm (red region), respectively. In summary, only Obregón et al. [34] observed a very frail emission band located at approximately 390 nm, which confirmed the up-conversion process proposed, whereby erbium converted the NIR photons to high-energy UV photons.

3.1.5. Photocatalytic properties of Er-TiO₂

The photocatalytic activity of the Er-TiO₂ photocatalysts was investigated under UV-vis, Vis and NIR irradiation using aqueous solutions of methylene blue (MB), phenol, methyl orange, rhodamine B, and orange I as model pollutants (see Table 1). These model reactions have been used to investigate both the effects of the erbium content incorporated into the TiO₂ structure as well as the calcination temperature on the photoactivity. Nonetheless, photocatalytic activity has been estimated using different set-ups and irradiation sources, such as 500 W xenon lamp, 200 W Hg-Xe lamp, deuterium-tungsten lamp, 160 W high-pressure mercury lamp, 8 W medium-pressure mercury lamp and light-emitting displays (LEDs) (Table 1). The effects of the erbium content incorporated into the TiO₂ structure and the calcination temperature on the photoactivity under solar simulated light using MB as the model pollutant was studied by Yang et al. [42]. It was shown that the photocatalytic activity of the erbium-doped TiO₂ was higher than that of pristine TiO₂ under simulated solar light [42]. The transition of the 4f electrons of Er³⁺ enhanced the optical adsorption of photocatalysts and benefitted the separation of photogenerated electron-hole pairs [42]. TiO₂ doped with 0.5 mol.% of erbium possessed the highest photocatalytic achievement, and the photoactivity diminished by increasing the doping dosage. It was stated that resulted lower photoactivity was due to higher number of recombination centers because surplus amounts of RE metals cover the surface of TiO₂ [42]. In the case of the calcination temperature, the authors observed that the photoactivity of the photocatalysts prepared from 400 to 700 °C decreased [42]. Combining these results with the crystalline phase of TiO₂, indicates that the presence of the rutile phase (detectable under a higher calcination temperature) was responsible for the lower photocatalytic activity in the photodegradation of organic compounds [42]. Reszczynska et al. [8] reported characteristics of Er-TiO₂ photocatalysts obtained via hydrothermal and sol-gel route. A high photocatalytic performance in the phenol photodegradation under visible light irradiation ($\lambda > 420$ nm) was observed for photocatalysts prepared by the hydrothermal method [8]. All RE-TiO₂ samples synthesized by the hydrothermal method had higher BET surface area and lower crystallite size than that developed by the sol-gel technique. Notwithstanding, photocatalysts prepared by the sol-gel method contained higher amounts of RE₂O₃ on their surfaces and fewer OH⁻ groups and Ti³⁺ moieties than the powders produced via the hydrothermal method [8]. The effect of the erbium content incorporated into the TiO₂ structure on the photoactivity was also investigated by Zheng and Wang [46]. They found that the optimal dopant loading equaled to 1 mol.%, which correspond to the maximum photocatalytic degradation rate [46]. Furthermore, the photodegradation of rhodamine B and phenol under LED irradiation ($\lambda = 517\text{--}522$ nm) demonstrated that Er-TiO₂ photocatalysts can show photocatalytic activity under visible light beyond the absorption edge of TiO₂. Obregón et al. [34] studied the photocatalytic performance of the Er-TiO₂ photocatalysts in the model reactions of phenol and MB in the aqueous phase and toluene in the gas phase degradation in the presence of irradiation with different spectral ranges of the lamp (UV, Vis and/or NIR). In this study, better photon efficiencies have been found for the reaction under NIR irradiation than under UV conditions. UV-induced photoactivity was assigned to electrons trapping by Er³⁺ ions working as scavengers, while photocatalytic activity under NIR was ascribed to the up-conversion properties of the Er-TiO₂ photocatalysts, resulting in pumping photons in the UV range into the TiO₂ structure. Castaneda-Contreras et al. [31] studied Er-TiO₂ photocatalysts prepared by the sol-gel method in the reaction of MB

degradation under visible light. They suggested that incorporation of erbium into the structure induces a marked red shift and a subsequent narrowing of the band gap values [31]. The improvement of the photoactivity was mainly attributed to the narrower band gap and, to a lesser extent, to energy transfer from Er³⁺ to TiO₂ [31]. To evaluate the photocatalytic activity of as-prepared samples, the kinetics of orange I photocatalytic depletion using Er-TiO₂ photocatalysts has been studied [33]. The obtained results demonstrated that the degradation and mineralization of orange I under both UV and visible radiation were more efficient in the presence of Er-TiO₂ photocatalysts than in the presence of pristine TiO₂. The authors concluded that the higher activity upon visible light might be attributed to the transition of the 4f electrons of Er³⁺ and the red shifts of the optical absorption edge of TiO₂ by erbium ion doping [33]. Bhethanabotla et al. [49] studied Yb/Er-TiO₂ photocatalysts in the reaction of phenol and Rose Bengal photodegradation under simulated solar irradiation and irradiation at different narrow wavelengths (405, 530, 660 and 940 nm). They observed that phenol and Rose Bengal was degraded only by irradiation using wavelength equaled to 405 nm. The enhanced photoactivity was described to photon energy of the excitation source relative to the band-gap and differences in defect chemistry instead of to up-conversion effect. On the other hand, Pickering et al. in their investigation [50] displayed that neither up-conversion decreased recombination rate nor band gap modification, but increased contaminants adsorption at the surface of photocatalysts was the most important reason for the improved performance of erbium based-TiO₂.

Finally, to enhance visible light response of Er-TiO₂ and thus photodegradation of pollutants, some additional modifications of these photocatalysts have been applied, such as carbon-sensitization and Fe-Er co-doping [51], Er-Yb co-doping [52] and composite systems, including YAG:Yb³⁺,Er³⁺/TiO₂ [50], YSO:Pr³⁺/TiO₂ and YAG:Er³⁺/TiO₂ [53].

3.2. Holmium-TiO₂

The structural, physical and photocatalytic properties of Ho-TiO₂ photocatalysts are summarized in Table 2. To develop Ho-TiO₂ photocatalysts in the form of zero-dimensional (nanoparticle) and one-dimensional (nanowire) morphologies, two most common methods, namely, the sol-gel and hydrothermal methods, respectively (see the third column in Table 2), have been employed. Regarding the morphology of Ho-TiO₂, Cai et al. [54] found that the Ho-TiO₂ nanoparticles had relatively uniform spherical grains, a narrow size distribution, and good dispersity compared with pristine TiO₂ nanoparticles, indicating that holmium doping could improve the particle morphology and hinder the grain growth of TiO₂ upon heat treatment. Also in the case of photocatalysts prepared by Shi et al. [55] the particle diameter of holmium-doped TiO₂ was smaller than pristine TiO₂, and moreover Ho-doped TiO₂ presented an anomalistic sphericity. Zhou et al. [56] described Ho-TiO₂ photocatalysts in the form of nanowires made using hydrothermal route. They found that nanowires with a uniform dispersion and with an outer diameter and length of 15 nm and 500 nm, respectively, have been formed at 150 °C [56]. Regarding the crystal structure, similarly to Er-TiO₂, holmium doping effectively inhibits the further transformation from anatase to rutile. The inhibition of the phase transition might be ascribed to the stabilization of the anatase phase by the surrounding rare earth ions through the Ti–O–Ho interaction [54,55]. It was also observed that the crystallite size of the Ho-TiO₂ decreased with an increase in the holmium doping amount [54]. Furthermore, studies have shown that the crystallite size increased with the increase of calcination temperature, which implied that holmium doping inhibited the growth of the crystallite size [55]. Shi et al. [55] stated that the BET surface area also increased after holmium doping due to the decrease of the crystallite size. Another important aspect of Ho-TiO₂ photocatalysts is the disturbing of band gap structure. Shi et al. [57] observed a tiny blue shift

Table 2
The structural and physical properties of the Ho-TiO₂ photocatalysts and description of photocatalytic system used to estimate photocatalytic activity.

No.	Preparation method/obtained structure	Localization of RE species	Chemical characteristics of RE species	Unit cell parameters	BET Surface area (m ² /g)	Band gap (eV)	Photocatalytic activity set -up	Up-conversion measurements	Ref.
1.	Sol-gel	Doping	Ion	0.1360 - pristine TiO ₂ 0.1365 - Ho-TiO ₂	No data	No data	Model contaminant: methyl orange	Not tested	[54]
2.	Sol-gel	Doping	Ion	0.1225 - pristine TiO ₂ 0.1235 - Ho-TiO ₂	No data	No data	Irradiation source: Mercury lamp Model contaminant: methyl orange	Not tested	[57]
3.	Sol-gel	Doping	Ion	0.1234 - pristine TiO ₂ 0.1245 - Ho-TiO ₂	38.42 - pristine TiO ₂ 76.76 for - Ho-TiO ₂	No data	Irradiation source: 500 W high-pressure mercury lamp Model contaminant: methyl orange	Not tested	[55]
4.	Hydrothermal Nanowires	Doping	Ion	No data	No data	No data	Irradiation source and range: 500 W high-pressure mercury lamp Model contaminant: methylene blue	Not tested	[56]
5.	Anodization	Surface doping	Oxide	136.64 - pristine TiO ₂ 136.73 - Ho-TiO ₂	No data	3.35 - pristine TiO ₂ 3.30 - Er-TiO ₂	Model contaminant: Phenol and toluene Irradiation source and range: 1000 W Xe lamp and LEDs (465 nm)	$\lambda_{\text{ex}} = 375, 530, 650$ and 980 nm $\lambda_{\text{em}} = \text{not observed}$	[10]

of the absorption profile in the Ho-TiO₂ compared to pristine TiO₂. This blue shift was also observed by Cai et al. [54] and was ascribed to the quantum size effect because Ho-doping greatly suppressed the crystal size of TiO₂. In contrast, a slight red shift of the absorption profile in the range of 300–450 nm was observed in the Ho-TiO₂ nanowires by Zhou et al. [56]. The authors ascribed these results to the charge transfer transition between the f electrons of Ho³⁺ ions and the TiO₂ conduction or valence band. The absorption edge shifted to a longer wavelength, which was dependent on the amount of Ho³⁺ incorporated into TiO₂ lattice [56]. According to the available literature, the photocatalytic properties of the Ho-TiO₂ photocatalysts were investigated mainly only upon UV-vis irradiation using a high-pressure mercury lamp as an excitation source and using dyes (methyl orange and MB) as the model pollutants (see Table 2). In all the studies, the photocatalytic activity of the Ho-TiO₂ photocatalysts was obviously higher than that of pristine TiO₂ [10,54]. The better performance of Ho-TiO₂ has been explained by the fact that the Ho-doped photocatalysts have a smaller crystallite size and can enhance the separation efficiency and inhibit the recombination efficiency of the photogenerated electron-hole pairs [56,57]. Moreover, the expansion in the crystal matrix creates oxygen vacancies, which generate shallow energy states at the bottom of the conduction band and serve as electron-trapping sites in TiO₂ [54]. Meanwhile, shallow energy states introduced by Ho ions in the top valence band served as hole-trapping sites. The separation of the charge carriers was attributed to this trapping mechanism [56]. The optimal dopant amount equaled to 0.3 mol.% for the maximum photocatalytic degradation rate when Ho-TiO₂ was calcined at 500 °C, and the optimal calcination temperature was 600 °C when the holmium amount was 0.5 mol.% [54–57].

3.3. Thulium-TiO₂

There are only a few studies regarding thulium-doped or co-doped materials in different applications [58–61], although Tm-TiO₂ photocatalysts have received very little research attention (see Table 3). Tm-doped TiO₂ photocatalysts were synthesized using a low-temperature hydrolysis reaction [62,63] as well as a ball-milling method [64]. The effects of the annealing temperature as well as thulium doping amount on the structural and electronic properties of the obtained Tm-TiO₂ materials were investigated. Navas et al. [62] noted that anatase was the predominant phase in the Tm-TiO₂ samples annealed at 500 and 700 °C, while rutile was the main phase in the samples annealed at 900 °C. It is worth noting that the authors observed only the phase corresponding to TiO₂ for the samples annealed at 500 and 700 °C, while in the case of the sample annealed at 900 °C, the pyrochlore phase of Tm₂Ti₂O₇ was also obtained [62]. Santos et al. [63] showed that mixed oxides of Tm and Ti were formed in the case of the Tm-TiO₂ photocatalyst annealed at 900 °C. Therefore, the Tm³⁺ ion may be incorporated into the anatase structure but not into the rutile one, probably because the ionic radius of Tm³⁺ is considerably larger than that of Ti⁴⁺ and the anatase structure is less dense than the rutile one [62]. A similar observation was reported by Shlyakhtina et al. [65] who showed that, for RE₂Ti₂O₇ (where RE = Lu, Yb, Tm) samples, the pyrochlore structure was formed at temperature higher than 800 °C [8]. Thus, all the above studies indicated that the structure of the Tm-doped TiO₂ nanoparticles can be thermally controlled. Modification of titania with thulium led to an increase in the BET specific surface area of the obtained photocatalysts, but it was not the primary factor for improving the photocatalytic activity of Tm-doped TiO₂ samples [63,64]. Furthermore, XPS analysis confirmed the presence of Tm³⁺ in the Tm-TiO₂ samples, which led to the generation of structural distortions and oxygen vacancies to maintain the local neutrality in the lattice [62–64]. The presence of Tm³⁺ in the samples also influenced the changes in the UV-vis absorption spectra, probably because of the presence of new states in the band gap, which produces a new photonic absorption process and shows photoluminescence properties [62]. Santos et al.

Table 3
The structural and physical properties of the Tm-TiO₂ photocatalysts and description of photocatalytic system used to estimate photocatalytic activity.

No.	Preparation method/ obtained structure	Localization of RE nanoparticles	Doping (substitutional)	chemical characteristics of RE species	Unit cell parameters	BET Surface area (m ² /g)	Crystallite size (nm)	Band-gap (eV)	Photocatalytic activity	Up-conversion measurements	Ref.
1.	Low temperature hydrolysis			Ion, oxidation state	V = 135.9 Å -pristine TiO ₂ V = 128.9 Å-Tm-TiO ₂	117.2-pristine TiO ₂ 274.6-Tm-TiO ₂	13.1 - pristine TiO ₂ 5-Tm-TiO ₂	3.01-pristine TiO ₂ 3.11-Tm-TiO ₂	Model contaminant:methylene blue	Not tested	[62]
2.	Ball mill/ nanoparticles		Doping (substitutional)	Oxidation state	V = 62.1-pristine TiO ₂ V = 135.9 Å-Tm-TiO ₂	24.6-pristine TiO ₂ 51.8-Tm-TiO ₂	57.2-pristine TiO ₂ 28.8-Tm-TiO ₂	2.98-pristine TiO ₂ 2.93-Tm-TiO ₂	Irradiation source and range: 5 actinic lamps (λ = 360 nm) Irradiation source and range: actinic lamp (λ = 360 nm)	Not tested	[63]
3.	Water-controlled hydrolysis reaction/ nanoparticles		Doping (substitutional)	Ion, oxidation state	V = 62.4-pristine TiO ₂ V = 62.5 Å-Tm-TiO ₂	20.2-pristine TiO ₂ 23.0-Tm-TiO ₂	69.9-pristine TiO ₂ 59.6-Tm-TiO ₂	2.96-pristine TiO ₂ 2.96-Tm-TiO ₂	Model contaminant:methylene blue Irradiation source and range: actinic lamps emitting (λ = 360 nm)	Not tested	[64]

[63] showed that Tm-doped samples presented several absorption bands centered at approximately 466, 685 and 785 nm, which corresponded to the transitions of Tm³⁺. A similar observation was reported by Navas et al. [62], who showed that the intensity of these three absorption peaks increased with higher amounts of neodymium in Nd-doped TiO₂ samples. The photocatalytic activity of Tm-doped TiO₂ and pristine TiO₂ nanoparticles was estimated by examining the reaction of MB degradation under UV light irradiation using an actinic lamp emitting at approximately 360 nm [62–64]. Navas et al. [62] investigated the photocatalytic efficiency of pristine rutile TiO₂ as well as 2 and 4.3 at.% Tm-doped TiO₂ samples, which are composed of the rutile and anatase TiO₂ as well as pyrochlore Tm₂Ti₂O₇ phases. It was observed that the rate of the photocatalytic reaction using the thulium-doped TiO₂ samples was approximately 50% faster than the reaction using non-modified TiO₂. The higher photocatalytic efficiency of the doped samples was ascribed to the formation of heterojunction at the interface of the phases in the thulium-doped samples, which promotes the separation of the electron-hole pair as well as the good charge carrier mobility due to the presence of the pyrochlore phase. These experimental results were also confirmed by theoretical calculations, which revealed that the Ti–O–Ti angle in the pyrochlore phase was approximately 136° (Fig. 4a), and this property influenced the high photocatalytic activity of the pyrochlore phase because charge carriers can move easily in the lattice. Importantly, the charge density and ELF studies (Fig. 4b and c) displayed that the presence of the Ti–O–Ti bonds enabled good charge mobility in the pyrochlore phase [62]. Santos et al. [63] investigated the influence of the annealing temperature of Tm-doped TiO₂ samples on the photocatalytic activity. It was interesting to note that samples annealed both at 500 and 720 °C exhibited lower photoactivity than pristine TiO₂. However, all Tm³⁺-doped samples annealed at 900 °C exhibited a significant improvement in the photoactivity (up to 94% degradation), 40% higher than the undoped TiO₂ [63], which was caused by the formation of a mixture of anatase, rutile and new pyrochlore Tm₂Ti₂O₇ phases [63]. In another study, the photocatalytic activity of the Tm-doped samples annealed at 900 was analyzed, and the reaction rate increased by a factor of 2.35 in the sample with 2.0 at.% Tm [64]. This result could be ascribed to the presence of pyrochlore, which is coincided with previous studies [62,63].

3.4. Neodymium-TiO₂

Different methods for the preparation of Nd³⁺-doped photocatalysts have been proposed: sol gel [66–76], a microwave-assisted mild temperature route [77], low-temperature synthesis [78] as well as chemical co-precipitation peptization [79] and hydrothermal methods [80], as shown in Table 4. Up to this moment, the effect of the Nd content on the physical structure and photocatalytic activities of doped samples was systematically investigated. Wojcieszak et al. [71] observed that an increase in the neodymium amount in the Nd-TiO₂ samples resulted in an increase in the crystallite size of the photocatalysts. In contrast, Khalid et al. [81], as well as El-Bahy and co-workers [68], suggested that Nd doping might restrain the growth of the TiO₂ crystallites. In another study, Wang et al. [78] showed that titania crystallites decreased in size as the amount of doped neodymium ions increased, which was explained by the adsorption of the neodymium species on the surface of titania, resulting in the inhibition of TiO₂ crystallite growth. The differences in the ionic radii prevent the neodymium ions from effectively being incorporated into the crystal structure of TiO₂; thus, neodymium is probably localized at the surface of the TiO₂ nanocrystals [71,80]. It is also worth noting that the negligible change in the cell parameters and cell volume of the doped samples compared to pristine TiO₂ also implied that neodymium ions were dispersed on the surface of TiO₂ [66,74]. Moreover, Gomez et al. [77] showed that the incorporation of Nd modified the BET surface area of Nd-TiO₂ samples, depending on the number of Nd ions. Low loadings of Nd significantly

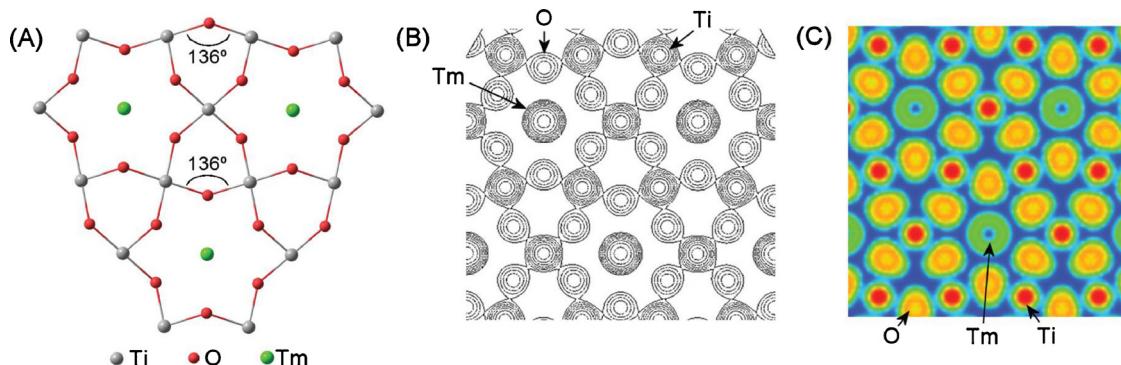


Fig. 4. (a) The local geometry, (b,c) analysis of the charge density and ELF for the pyrochlore phase ($\text{Tm}_2\text{Ti}_2\text{O}_7$) [62]. Reprinted with permission from ref [62]. Copyright 2014 The Royal Society of Chemistry.

increased the TiO_2 surface area, which was in good agreement with the results obtained by Hewer et al. [67] and Bokare et al. [66]. In contrast, a larger amount of Nd reduced the TiO_2 BET surface area, probably due to the blockage of some of the pores by the Nd clusters [77]. Kralchevska et al. [72] showed that modification of TiO_2 with neodymium significantly influenced the material texture, leading to increases in the BET surface area and micropore volume. It was also reported that modification of titania with neodymium greatly affected the light absorption property of the photocatalysts. Xu et al. [75] showed that the introduction of Nd extended the absorption spectrum of TiO_2 into the visible region and decreased the titania band gap, which was assigned to the charge transfer between the Nd ion 4f level and the titania conduction or valence band. A similar observation was obtained by Wang et al. [78], who reported enhanced absorption properties of Nd- TiO_2 samples compared to pristine TiO_2 and observed five typical absorption peaks located at 527, 586, 762, 809 and 862 nm, which could be related to the 4f electron transitions or the f-f transition of the Nd ions.

Furthermore, it was shown that doping by neodymium can affect the morphology of the TiO_2 particles. Bokare et al. [66] observed that undoped TiO_2 presented irregularly sized and shaped particles, while in the case of Nd-doped samples, particles with a more uniform size and shape were observed. Wojcieszak et al. [71] showed that undoped titania nanoparticles formed agglomerates, while the incorporation of the neodymium dopant in the amounts of 1 at.% and 3 at.% caused the TiO_2 agglomerates to become smaller. The addition of neodymium ions has been shown to increase the photocatalytic activity of titania for the removal of methyl orange [66,67,71,75], phenol [80,77,79], Remazol black B [79], direct blue 53 [68], reactive brilliant red X-3B [78], 2-mercaptopbenzothiazole [70], malachite green [72], and rhodamine B [76], as well as the photoreduction of chromium (VI) [74] (see Table 4). It was reported that an appropriate amount of Nd-dopant played a crucial role in determining the photocatalytic activity of Nd- TiO_2 samples toward methyl orange decomposition, and an optimum amount of dopant in this system equaled to 3 at.% neodymium [71]. Bokare et al. [66] revealed that the highest activity was observed for TiO_2 containing 1 at.% of Nd, which was 30% higher than for the undoped TiO_2 . A similar result was obtained by Khalid and co-workers [81], who showed that the best photoactivity was recognized for a 1 at.% Nd- TiO_2 sample. It is also interesting to note that Gomez et al. [77] reported that the main factors affecting the phenol degradation were the amount of neodymium and the band gap structure, while the surface area was the crucial parameter in the case of rhodamine B degradation. Wang et al. [78] proposed a photocatalytic mechanism of Nd-doped TiO_2 in which the excited electron can transfer from the valence band of TiO_2 to the newly formed neodymium energy levels below the conduction band of titania and can, therefore, be activated by visible light. Additionally, modification of TiO_2 with neodymium led to defects in the lattice, which acted as electron traps, resulting in an enhanced separation of

charge carriers [78]. This result was in good agreement with the results obtained by Nassoko et al. [76], who reported that Nd entered into the TiO_2 lattice, and under visible light irradiation, the electrons were excited from the valence band to the $\text{Nd}^{3+}/\text{Nd}^{2+}$ doping energy level. Additionally, it was found that hydroxyl radicals, as one of the reactive species, were produced by photogenerated electrons both from Nd-doped titania and rhodamine B and were mainly responsible for the photodegradation of the dye molecules [76]. In another study, Parnicka et al. [80,82] performed measurements of photocatalytic degradation in the presence of scavengers, and the results implied that e^- and O_2^- were responsible for the photocatalytic degradation of phenol in the presence of Nd- TiO_2 samples under visible light irradiation. Furthermore, the action spectra analysis showed that Nd- TiO_2 samples could be activated by visible light with a wavelength range from 400 to 480 nm, suggesting that the up-conversion process of visible to ultraviolet light was not responsible for the visible light-driven photoactivity of Nd- TiO_2 photocatalysts [80].

4. The origin of RE- TiO_2 visible light photoactivity

4.1. Theoretical study of lanthanides- TiO_2 photocatalysts

4.1.1. Basic principles of the theoretical study of lanthanides- TiO_2 photocatalysts

Quantum chemical calculations are inexpensive and fast methods that can provide a description of the electronic and optical properties of surface-modified TiO_2 systems at the design stage (before synthesis) of new photocatalysts. The results from these theoretical calculations might provide important information for understanding and predicting the influence of RE metals on the electronic and atomic structure of RE-doped TiO_2 properties [83]. The most promising approaches that can be applied for this purpose are related to density functional theory (DFT methods) [83]. DFT theory can overcome the challenge related to investigating electronic structures in solid-state physics; more importantly, it is an effective approach for predicting the trend of the energy gap variation in doped semiconductors [83]. Despite the extensive experimental studies of RE- TiO_2 (as shown in Tables 1–4), there is a serious problem in the description of the effects of impurities on the TiO_2 photocatalyst performance. Thus, theoretical groups have reported numerous calculations to predict the properties of the complex RE- TiO_2 systems to provide more valuable insight into the experimental preparation that could improve the photoresponse activity from the UV to the Vis light region (as summarized in Table 5). On the basis of the first-principles calculations, the theoretical results show that the localized 4f states of lanthanide ions (RE^{3+}) commonly result in band gap narrowing and photoresponse improvements under the visible light region [10,84]. Thus, in this part, we summarized the theoretical calculation of the electronic structure, charge density, and optical properties of RE^{3+} -doped TiO_2 systems. The mechanism of the enhanced

Table 4
The structural and physical properties of Nd-TiO₂ photocatalysts and description of photocatalytic system used to estimate photocatalytic activity.

No.	Preparation method / obtained structure	Localization of RE species	Chemical characteristics of RE species	Crystallite size (nm)	BET Surface area (m ² /g)	Unit cell parameters	Band-gap (eV)	Photocatalytic activity	Up-conversion measurements	Ref.
1.	Sol-gel/ nanoparticles	Doping (interstitial)	Ion, oxide	20.759- TiO ₂	108.7 - pristine TiO ₂	a = 3.786 nm, b = c = 9.507 nm, V = 136.315 Å ³ - pristine TiO ₂	No data	Model contaminant:methyl orange	$\lambda_{ex} = 345$ nm	[66]
2.	Mild microwave-assisted/ nanoparticles	Doping (interstitial)	Ion	7.598- Nd-TiO ₂	123.4 - Nd-TiO ₂	a = 3.778 nm, b = c = 9.532 nm,	Irradiation source and range: direct sunlight (4% UV and 43% visible light)	λ_{em} :~ 410,~ 450,~ 475	[77]	
3.	Sol-gel and precipitation/ nanoparticles	Doping	Ion, oxide	6.92 - pristine TiO ₂	239 - pristine TiO ₂	V = 136.629 Å ³ - Nd-TiO ₂ a = 3.80 Å, c = 9.64 Å - pristine TiO ₂	2.95 - pristine TiO ₂	Model contaminant:phenol	Not tested	[67]
4.	Sol-gel/ nanoparticles	Doping	Ion, oxidation state	5.79 - Nd-TiO ₂	258- Nd-TiO ₂	a = 3.80 Å, c = 9.61 Å - Nd-TiO ₂	2.89- Nd-TiO ₂	Irradiation source and range: medium pressure mercury lamp (λ_{max} = 365 nm).	[68]	
5.	Sol-gel/ monolith	Doping (substitutional) and intercalation	Ion	19.3 - pristine TiO ₂	81 - pristine TiO ₂	No data	No data	Model contaminant:benzene	Not tested	[69]
6.	Sol-gel	Doping	Ion	12.3 - Nd-TiO ₂	127.1- Nd-TiO ₂	29.5 - pristine TiO ₂	3.27- pristine TiO ₂	Irradiation source and range: high pressure mercury lamp (λ < 400 nm)	[70]	
7.	Sol-gel/ nanoparticles	Doping	Ion	22.6- Nd-TiO ₂	31.2- Nd-TiO ₂	223- pristine TiO ₂	3.25- Nd-TiO ₂	Model contaminant:direct blue 53	Not tested	[71]
8.	Sol-gel	Doping	Ion, oxidation state	74.9 - Nd-TiO ₂	74.9 - Nd-TiO ₂	No data	3.10 - pristine TiO ₂	Irradiation source and range: xenon lamp (λ > 320 nm)	[72]	
9.	Sol-gel	Doping	Ion	32.9 - pristine TiO ₂	50.2- pristine TiO ₂	2.96 - Nd-TiO ₂	No data	Model contaminant:orange	Not tested	[73]
				19.8 - Nd-TiO ₂	78.5 - Nd-TiO ₂	No data	2.96 - Nd-TiO ₂	Irradiation source and range: Xenon lamp (λ > 365 nm)		
				4.2 - pristine TiO ₂	No data	No data	No data	Model contaminant: 2-mercaptobenzothiazole		
				4.6- Nd-TiO ₂	No data	No data	No data	Irradiation source and range: medium-pressure mercury lamp (λ = 365 nm)		
				7.6- Nd-TiO ₂	7.3 - pristine TiO ₂	a = 3.781 nm,	No data	Model contaminant: methyl orange		
				57.7- Nd-TiO ₂	c = 9.506 nm - pristine TiO ₂ a = 3.791 nm, c = 9.505 nm	λ_{ex} = 330 nm				
				32.9 - pristine TiO ₂	43.29 - pristine TiO ₂	- Nd-TiO ₂	No data	Irradiation source and range: UV lamp Sylvania, (345-400 nm, λ_{max} : 365 nm)		
				17.8- Nd-TiO ₂	90.91- Nd-TiO ₂	No data	No data	Model contaminant: 2-mercaptobenzothiazole		
						No data	No data	Irradiation source and range: high-pressure sodium lamp (400-800 nm)		

(continued on next page)

Table 4 (continued)

No.	Preparation method/ obtained structure	Localization of RE species	Chemical characteristics of RE species	Crystallite size (nm)	BET Surface area (m ² /g)	Unit cell parameters	Band-gap (eV)	Photocatalytic activity	Up-conversion measurements	Ref.
10.	Chemical coprecipitation–peptization/nanoparticles	Doping	Ion	No data	No data	No data	6	Model contaminant: phenol Irradiation source and range: halogen-tungsten lamp (400–800 nm, $\lambda_{\text{max}} = 550 \text{ nm}$)	Not tested	[79]
11.	Sol-gel/ nanoparticles	Doping	Ion	15.84 - pristine TiO ₂ 6.19- Nd-TiO ₂	No data	a = 0.38 nm	No data	Photocatalytic reaction: reduction of Cr(VI) Irradiation source and range: medium-pressure mercury lamp (325 nm)	Not tested	[74]
12.	Low temperature/ hollow spheres	Doping	Ion, oxide	No data - pristine TiO ₂ 8.9- Nd-TiO ₂	No data	c = 0.95 nm - pristine TiO ₂ a = 0.38 nm c = 0.95 nm- Nd-TiO ₂	No data	Model contaminant: reactive brilliant red X-3B Irradiation source and range: 250 W halogen lamp ($\lambda > 400 \text{ nm}$) Efficiency: 60.9% after 100 min	Not tested	[78]
13.	Sol-gel and hydrothermal/ nanotubes	Doping (interstitial)	Ion, oxide	No data	No data	No data	No data	Model contaminant: methyl orange Irradiation source and range: high-pressure mercury lamp	Not tested	[75]
14.	Sol-gel/ nanoparticles	Doping (interstitial)	Ion, oxide	20.32 - pristine TiO ₂ 20.35- Nd-TiO ₂	72.46 - pristine TiO ₂ 59.54- Nd-TiO ₂	No data	Model contaminant: rhodamine B Irradiation source and range: Xenon Lamp ($\lambda > 420 \text{ nm}$)	Not tested		[76]
15.	Hydrothermal	Doping	Ion, oxide	18.8 - pristine TiO ₂ 10.9- Nd-TiO ₂	107 - pristine TiO ₂ 124- Nd-TiO ₂	No data	Model contaminant: phenol Irradiation source and range: Xenon Lamp ($\lambda > 420 \text{ nm}$)	Not tested		[80]

Table 5Computational details for the computed RE-TiO₂ structures available in the literature.

Type of structure	The k-point meshes used for geometrical optimizations	The plane-wave energy cutoff	The structural energy convergence/ the forces of relaxation	The valence atomic configurations	Methods	Software	Ref.
Nd ₂ TiO ₂ O ₇	4 × 4 × 4 4 × 4 × 2 4 × 4 × 1	500 eV	self-consistent convergence of the total energy/ 0.01 eV/Å	Nd (5s25p66s25d1) Ti (3s23p63d24s2) O (2s22p4)	DFT-GGA + U (U = 7 eV) with PW	VASP	[88]
Nd ³⁺ -TiO ₂	Not provided	Not provided	Not provided	Not provided	DFT	Not provided	[84]
Tm _x Ti _{1-x} O ₂	x 7 × 3 2 × 3 × 3 x 3 × 3 2 × 4 × 1 8 × 8 × 11 3 × 7 × 1 2 × 2 × 1	400 eV	5.0 × 10 ⁻⁷ eV/atom/ 0.01 eV/Å	Tm (4f13 5s25p66s2) Ti (3s23p63d24s2) O (2s22p4)	DFT/ GGA with PAW	CASTEP	[89]
Ho-TiO ₂	8 × 8 × 11 3 × 7 × 1 2 × 2 × 1	400 eV	< 1 meV/atom < 0.02 eV Å	Ho (4f11s25p66s2) Ti (3s23p63d24s2) O (2s22p4)	DFT/ GGA with PAW	VASP	[10]

band gap narrowing and the associated optical properties are also discussed in this section. It could be noted that up to this moment theoretical investigations on RE = Nd³⁺, Tm³⁺, Ho³⁺, Er³⁺ doping are relatively rare.

4.1.2. Computational characterization of the investigated RE-TiO₂ structures

One of computationally investigates RE-TiO₂ system (i.e., Nd₂Ti₂O₇) was provided by Bruyer and Sayede in 2010 [85]. The authors indicated that the Nd₂Ti₂O₇ system could be applied in the water-splitting reaction and they reported the results from DFT methods on the structural optimization for Nd-TiO₂ in different atomic arrangements (Table 5) [85]. The room temperature arrangement of the investigated structure was monoclinic P2₁ with the lattice constants $a = 13.02 \text{ \AA}$, $b = 5.48 \text{ \AA}$, $c = 7.62 \text{ \AA}$ and $\beta = 98.28^\circ$. Bruyer and Sayede [85] provided results on the chemical bonding, structural phase stability and ferroelectronic properties, as well as the electronic structure of the Nd-TiO₂ system. The electronic structures of Nd₂Ti₂O₇ have been studied using the general gradient approximation method (GGA + U method). Based on GGA + U calculations and the density of states (DOS), the authors suggested a half-metallic nature for Nd₂Ti₂O₇ [85]. These results do not correspond to the experiment provided by Hwang et al. [86]. However, the GGA + U results moved the Nd 4f states away from the E_F, yielding an insulating ground state. The localized Nd 4f levels at the top of the valence band (VB) and at a lower position in the conduction band (CB) acted as charge-trapping sites, showing that the Nd₂Ti₂O₇ structure had a reduced photocatalytic activity [85]. Li et al. [87] observed band gap narrowing for the 0%, 1% and 1.5% Nd³⁺-doped TiO₂ nanoparticles (NPs). To interpret the band gap (E_g) changes, the authors used the generalized gradient approximation (GGA) with the linearized augmented plane wave method (LAPW). The Nd-doped anatase was modeled by a structurally optimized NdTi₇O₁₆ supercell with Nd³⁺ in a substitutional site. Li et al. [87] indicated that the band gap narrowing was primarily attributed to the substitutional Nd³⁺ ions. Based on the obtained calculations, the authors indicated that Nd³⁺ ions introduced electron states into the band gap of TiO₂ (~ 2.26 eV), and these electron states influenced the new lowest unoccupied molecular orbitals (LUMOs). The calculated band gap of pristine TiO₂ equal to 1.97 eV, with the O 2p orbital states contribution at the top of the VB and the Ti 3d orbital contributions at the CB [87]. The calculated E_g of Ti₇NdO₁₆ that corresponds to 4 at.% Nd equal to 1.97 eV, and from the DOS analysis, the authors concluded that some electronic states, which were located close to the CB, were introduced into the band gap of TiO₂ by Nd 4f electrons to form the new LUMO [87]. Consequently, the absorption edge transition for the doped material can be from O 2p to Nd 4f instead of Ti 3d, as in pristine TiO₂. Li et al. [87] observed that the maximum band gap reduction (E_g = 0.55 eV) was found for 1.5 at.% Nd-doped TiO₂ nanoparticles. Based on the obtained results, the authors indicated that E_g narrowing could be related to the substitutional

Nd³⁺ ions, which introduced electron states into the band gap of TiO₂ to form the new LUMO [87].

Mazierski et al. [10] investigated the electronic structure and partial density of states (PDOS) of pristine TiO₂ and Ho-TiO₂. The electronic structure of the TiO₂ anatase system was changed by the defects in the photocatalyst surface and by the location of the Ho³⁺. The Ho f states exist in the band gap of defective anatase TiO₂(101). The authors observed the system stabilization after the formation of defects at the surface of the Ho-anatase TiO₂(101) [10]. Wei and Jia [84] reported the electronic structure, charge density and optical properties of Tm³⁺-modified TiO₂ based on DFT calculations (Table 5). The authors investigated three different configurations of the Ti_{1-x}Tm_xO₂ systems (see Fig. 5), in which the variation x was defined by the values of 0.0417, 0.0625, and 0.125. Tm atoms in Ti_{1-x}Tm_xO₂ systems were introduced into the regular Ti lattice position. The supercells were composed of multiples of the lattice vectors a , b , c , such as 3 × 2 × 1 (72 atoms), 2 × 2 × 1 (48 atoms), and 2 × 1 × 1 (24 atoms) supercells for the anatase phase Ti_{1-x}Tm_xO₂ system, which represented the doping concentrations of 1.39 at.% (Ti₂₃O₄₈Tm₁), 2.08 at.% (Ti₁₅O₃₂Tm₁) and 4.17 at.% (Ti₇O₁₆Tm₁), respectively [84]. The optical properties and electronic structures of the Tm-TiO₂ system were studied using the plane-wave DFT method with the Padrew-Burke-Ernzerhof-generalized gradient approximation functional (PBE/GGA) [84]. Wei and Jia [84] discussed the mechanism of the enhanced band gap (E_g) narrowing and the associated optical properties of the investigated Tm-TiO₂ system. Wei and Jia [84] observed the reduction of the band gap compared to pure anatase TiO₂ due to the incorporation of Tm into the anatase TiO₂ structure. The band gap was apparently reduced from 2.17 to 1.93 eV in the Tm-doped Ti₂₃O₄₈Tm₁ system. Consequently, Tm doping narrowed the band gap to a value of approximately $\Delta E_g = 0.24$ eV [84]. For the Tm-doped anatase Ti₁₅O₃₂Tm₁ and Ti₇O₁₆Tm₁, the band gap energies, i.e., 1.92 eV ($\Delta E_g = 0.22$) and 1.83 eV ($\Delta E_g = 0.29$), corresponded to the doping levels of 2.08 at.% and 4.17 at.% of Tm atoms, respectively. Moreover, the presented results indicated that the Tm atoms substantially modified the DOS, inducing variations in both the VB and the CB [84]. The authors observed that the substitutional Tm dopant increased the delocalized Tm 4f states above the VB, which narrows the band gap, resulting in a red shift of the optical absorption edges [84]. A dependency between the Tm concentration and the band gap reduction was observed. The presented study was the starting point for the designed band-gap reduction using Tm-doped TiO₂ for extending the optical absorption into the visible solar light region for improved photocatalytic performance [84].

From the considered examples discussed in this paper, it appears that the theoretical description at the DFT level of the RE-TiO₂ semiconductor oxides presents a number of problems. Obtaining more accurate defect formation energies and a more reliable distribution of the excess electrons requires going beyond the GGA in DFT by using hybrid approaches; in general, this means increasing the computational

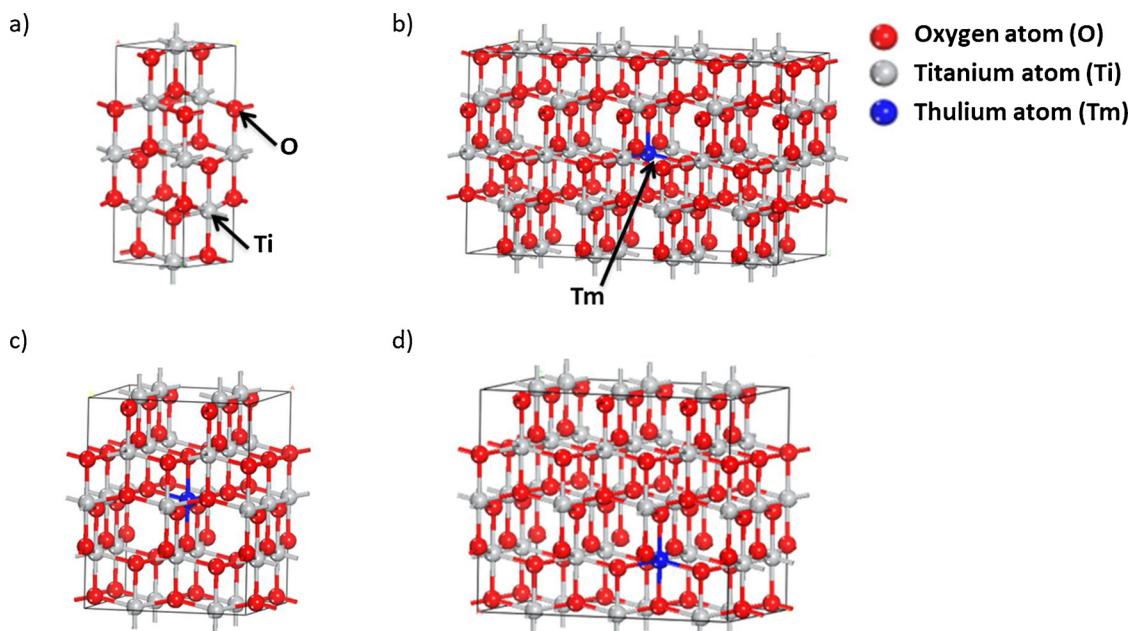


Fig. 5. The example investigated of the unit cell and doping model with substitutionally doped Tm atoms in the anatase TiO_2 supercells: (a) unit cell; (b) $3 \times 1 \times 1$ supercell; (c) $2 \times 2 \times 1$ supercell; and (d) $2 \times 1 \times 1$ supercell. The red, gray and blue spheres represent oxygen, titanium, and thulium atoms, respectively, based on [84]. Reprinted with permission from ref [84]. Copyright 2015 Society of Photo-Optical Instrumentation Engineers (SPIE) (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article).

demands. Thus, the choice of the model of the reduced system may become crucial. The question arises of whether widely used periodic models will be useful in this respect. Very recent studies on the electronic structure of defective $\text{TiO}_2(110)$ surfaces using periodic models and hybrid functionals in [90] and [91] indicate that an increased interest can be expected in this type of calculation in the near future. However, cluster approaches will still be useful (and less costly computationally). Nonetheless, a universal hybrid functional that includes a fixed amount of the exact exchange might not necessarily be able to describe the electronic structure of all (different) RE- TiO_2 structures with the same accuracy.

4.2. Anti-Stokes up-conversion process in the RE- TiO_2 mechanism

The simplified mechanism of the TiO_2 excitation by the up-conversion luminescence agent is presented in Fig. 6.

To explain the possible mechanism of lanthanide-modified TiO_2 excitation under visible light, the photodegradation of model pollutants should be investigated as a function of irradiation wavelength (action spectra (AS) analysis) [8]. Based on AS analysis, it is possible to determine which aspect of light absorbed by the photocatalyst is involved in the photocatalytic reactions [80]. If the up-conversion process is involved in the improvement of the photocatalytic activity under visible light, then an enhancement of the photocatalytic activity in RE absorption bands region should be observed. In the recent literature, there are only a few reports of RE- TiO_2 AS measurements. Parnicka et al. [80] investigated the influence of the irradiation wavelength on the photocatalytic activity of the phenol degradation reaction in the presence of Nd- TiO_2 photocatalysts. The AS of the samples did not resemble the Nd- TiO_2 absorption spectra. The Nd-modified TiO_2 photocatalyst showed photocatalytic activity under visible light in a continuous irradiation range from 400 to 480 nm [80]. Photocatalytic activity under the Nd absorption band wavelengths ($\lambda = 525, 585, 745$, and 805 nm) was not observed (Fig. 7).

No correlation between the wavelengths responsible for the photocatalytic activity and the absorption spectra of RE was also observed by Reszczynska et al. [9,11]; the photocatalysts Er-Yb- TiO_2 , Nd-Eu- TiO_2

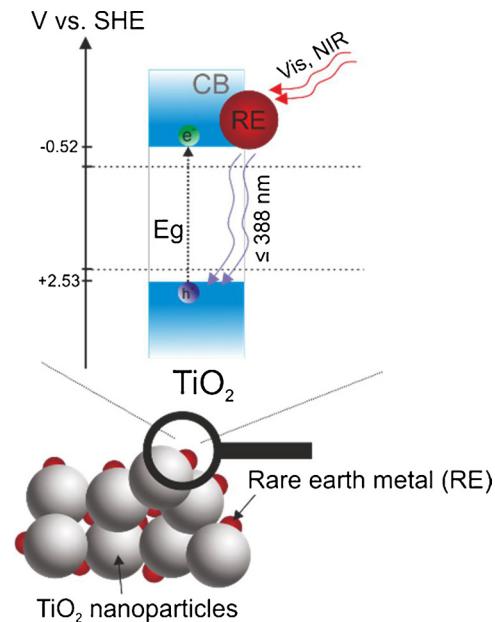


Fig. 6. Simplified mechanism of TiO_2 excitation by an up-conversion luminescence agent.

and Eu-Ho- TiO_2 showed photoactivity in the 420–475 nm, 420–450 nm and 420–450 nm regions, respectively. The enhancement of the photocatalytic activity under 488, 522, 524, 586 or 653 nm was not observed [9,11]. Different results have been obtained by Castaneda-Contreras et al. [31] who postulated that the up-conversion process in erbium ions was responsible for MB photodegradation under 532 nm laser beam light. According to recent literature, the reason that the impact of the up-conversion process on the photocatalytic activity was not always observed was because of the large distance between the ground and excited states of the RE ions (multiphoton excitation) and multiphonon

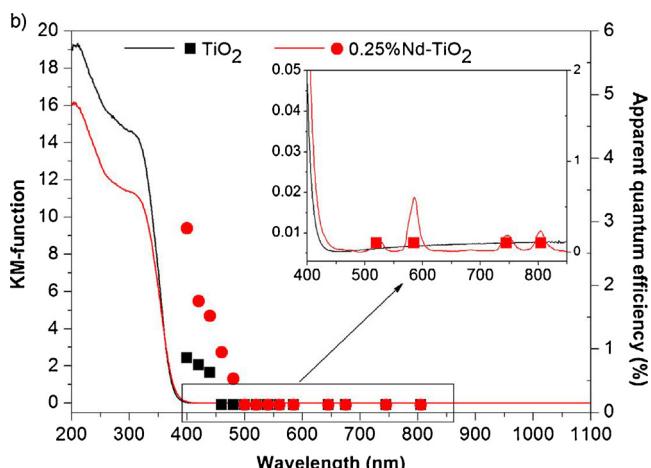


Fig. 7. Action spectrum of the photocatalytic degradation of phenol in the presence of neodymium-modified TiO_2 [80]. Reprinted with permission from ref [80]. Copyright 2017 Elsevier B.V.

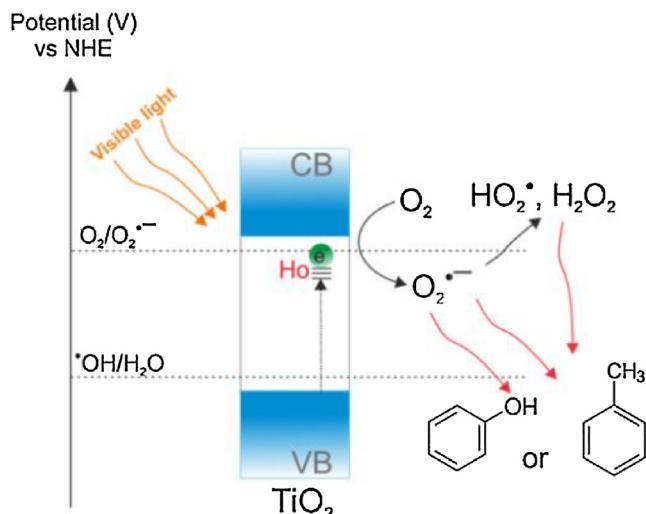


Fig. 8. Schematic illustration of the formation of sub-bandgap states below the conduction band of the TiO_2 semiconductor after the incorporation of Ho or Nd ions, based on [10,78]. Reprinted with permission from ref [10,78]. Copyright 2010, 2016 Elsevier B.V.

relaxation processes that were affected by the properties of the crystal structure of the photocatalysts [92,93]. Moreover, the aqueous environment of the solutions caused the interaction of RE with water (both in the inner and outer coordination spheres of the RE^{3+}) and led to a severe quenching of the RE luminescence via O–H vibrations [94]. The best way to minimize the water deactivation processes is to protect the RE^{3+} ion from solvent interactions, e.g., with a chelating process or by binding RE with peptides [94,95]. In the recent literature, there is no information regarding TiO_2 photocatalysts modified with RE ions with extra protection from aqueous interactions. Based on the literature, there is no reliable proof that the up-conversion process has a real impact on the RE- TiO_2 photocatalytic activity under visible light irradiation; therefore, this aspect should be clarified in the future. Mazierski et al. [10] and Wang et al. [78] stated that the incorporation of Ho or Nd ions into the TiO_2 structure leads to the formation of sub-bandgap states that lie below the CB of the semiconductor. The

electrons can be excited from the VB to the lanthanide 4f level under visible light irradiation (as shown in Fig. 8). These trapped electrons can react with O_2 and form reactive oxygen species, such as $\text{O}_2^{\cdot-}$, HO_2 and H_2O_2 , leading to organic pollutant degradation [10].

5. Conclusions and perspectives

Current review provides a comprehensive summary of the studies that investigated modification of TiO_2 with Er, Ho, Nd and Tm ions. Rare ions (RE) were used for the TiO_2 modification in order to obtain photocatalysts being active under visible light irradiation. In particular, dye degradation has been found to be a popular choice for the comparison of the photoactivity between pristine TiO_2 and RE- TiO_2 . The aforementioned literature data suggests that RE- TiO_2 modification is effective in increasing the photocatalytic activity of TiO_2 , especially at low loading levels. However, due to various photocatalytic activity set-ups chosen for the carried tests, the choice of a lanthanide causing the highest increase is challenging. According to the literature, there is no reliable proof that the up-conversion process has a real impact on the RE- TiO_2 photocatalytic activity under a visible light irradiation. Moreover, there is currently no information regarding TiO_2 photocatalysts modified with RE ions with extra protection from aqueous interactions in the recent literature. Therefore, those two aspects should be clarified in the future. What is more, time-consuming and often very expensive experimental testing, as well as substantial amount of the possible RE- TiO_2 structure combinations leads to limitations in proper characterization of RE- TiO_2 photocatalysts. It has been widely proved that theoretical calculations combined with chemoinformatics methods (i.e. Quantitative Structure-Property Relationship modeling, QSPR) may support the experimental testing of new potential photocatalysts [10,96–98]. However, an effective approach that combines theoretical and computational calculations with experimental design is still not well developed yet. Since organizing a synergistic interaction between experimentalists and theoreticians is a critical step, we proposed a roadmap (Fig. 9), showing which objectives need to be achieved in a short-, medium-, and long-term tasks. In the first step (i.e. short-term task) the following tasks are of highest importance: i) selection of well characterized materials for the experiments; ii) selection and measurements of activity-relevant endpoints (Fig. 9). When examining photocatalytic properties of RE- TiO_2 systems, it is important that electronic and atomic properties of TiO_2 , RE particles and RE- TiO_2 systems are well characterized and understood, so that valid inferences can be gained, and how these structure properties influence the photocatalytic activity. Therefore, in the second step (i.e. medium-term task), a computational approach should be undertaken, where one of the most important components of theoretical methods are developed. The physico-chemical features, defined as descriptors can help in understanding the relationships between atomic structure and electronic/optical properties of investigated molecular models. In the long-term task, the database comprised of physico-chemical properties (i.e. descriptors) and photocatalytic activity measurements (i.e. endpoints) of investigated TiO_2 systems should be developed. Afterwards, on a basis of the gathered data, computational models (i.e. QSPR models for nanoparticles, nano-QSPR) for reliable endpoints should be developed, providing a knowledge how the photocatalyst structure affects its desired property (i.e. photocatalytic activity). Finally, the developed models should be used to preliminarily estimate photocatalytic activity of new (untested) structures at early stage of experimental design. The long-term goal is to create nano-QSPR models of TiO_2 based structures, to generate sufficient experimental and mechanistic data for experimental researchers that will help deciding which structural features should be used and/or changed in order to design novel and efficient

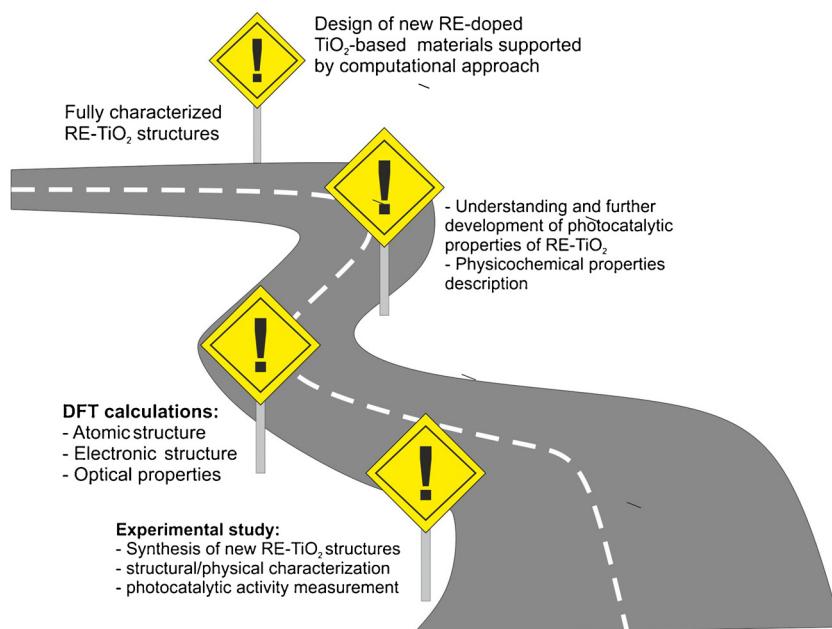


Fig. 9. Combined experimental and computational roadmap showing the objectives for first-principles calculations in supporting experimental procedures for the further design of new RE-TiO₂-based materials.

photocatalytic systems having desired properties (i.e. effective photocatalytic activity).

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